

**ASSIGNMENT SET - I****Department of Mathematics****Mugberia Gangadhar Mahavidyalaya****B.Sc Hon.(CBCS)****Mathematics: Semester-V****Paper Code: DSE1T****[Linear Programming]****Answer all the questions**

- 1) Define feasible solution and optimal solution of an L.P.P.
- 2) Verify graphically the following problem has an unbounded solution  
 Maximize  $Z = 3x_1 + 4x_2$   
 Subject to  $x_1 - 3x_2 \leq 3$ ,  $x_2 - x_1 \leq 1$ ,  $x_1 + x_2 \geq 4$  and  $x_1, x_2 \geq 0$ .
- 3) Distinguish between extreme point and boundary point with suitable example.
- 4) Define convex set. Give an example of a convex set in which all boundary points are vertices.
- 5) Write all the characteristics for the standard form of an L.P.P.
- 6) Construct the dual of the following L.P.P.  
 Maximize  $Z = 4x_1 + 9x_2 + 2x_3$   
 Subject to  $2x_1 + 3x_2 + 2x_3 \leq 7$ ,  $3x_1 - 2x_2 + 4x_3 = 5$  and  $x_1, x_2, x_3 \geq 0$ .
- 7) Determine the convex hull of the point (0,0), (0,1), (1,1), and (4,0).
- 8) Obtain one basic feasible solution of the system of equation  
 $x_1 + 4x_2 - x_3 = 5$ ,  $2x_1 + 3x_2 + x_3 = 8$
- 9) Does a basic contain a null vector? Give reasons for your answer.
- 10) When artificial variables are used for solving an L.P.P. by simplex method?
- 11) Show that the dual of the dual of an L.P.P. is the primal itself.

- 12) State the fundamental theorem of duality.  
 13) Define separating and supporting hyperplanes.  
 14) Under what condition an L.P.P. will have unbounded solution?  
 15) Prove that a hyperplane and a closed half space in  $E^n$  are unbounded closed convex sets.  
 16) If  $x + iy$  moves on the straight line  $3x + 4y + 5 = 0$ , then find the minimum value of  $|x + iy|$ .

**17)** Solve the following L.P.P. by graphical method:

$$\text{Minimize } Z = x_1 + 2x_2$$

$$\text{Subject to } 5x_1 + 9x_2 \leq 45, x_1 + x_2 \geq 2, x_1 \leq 4 \text{ and } x_1, x_2 \geq 0$$

- 18) Food X contains 7 unit of vitamin A and 5 units of vitamin B per gram and costs 20 p/gm. Food Y contains 12 units and 15 units of A and B per gram respectively and costs 50 p/gm. The daily requirement of vitamin A and vitamin B are at least 200 units and 320 units respectively. Formulate this problems as an L.P.P to minimize the cost.

- 19)  $x_1 = 1, x_2 = 1, x_3 = 2$  is a feasible solution of the equation

$$x_1 + 2x_2 + 3x_3 = 9$$

$$2x_1 - x_2 + x_3 = 3 \text{ and } x_1, x_2, x_3 \geq 0$$

- 20) Reduce the feasible solution to a basic feasible solution of the above system of equation.

- 21) Show that the set given by  $X = \{(x_1, x_2) : 9x_1^2 + 16x_2^2 \leq 144\}$  is a convex set.

- 22) Show that if either the primal or dual problem has a finite optimal solutions, then the other problem also has a finite optional solution and the values of the values of the two objective functions are equal.

23) Solve the following L.P.P.:

$$\text{Maximize } Z = 2x_1 + x_2 + x_3$$

$$\text{Subject to } 4x_1 + 6x_2 + 3x_3 \leq 8, 3x_1 - 6x_2 - 4x_3 \leq 1, 2x_1 + 3x_2 - 5x_3 \geq 4$$

$$\text{and } x_1, x_2, x_3 \geq 0.$$

- 24) ) i) Solve the following L.P.P. by using two phase simplex method

$$\text{Maximize } Z = x_1 + x_2$$

Subject to  $2x_1 + 4x_2 \geq 4$ ,  $x_1 + 7x_2 \geq 7$  and  $x_1, x_2 \geq 0$

ii) Show that the set of all feasible solution to an L.P.P. is a closed convex set.

25) Obtain the dual of the following L.P.P. and hence solve it

Maximize  $Z = 3x_1 + 4x_2$

Subject to  $x_1 + 4x_2 + 2x_3 \geq 5$ ,  $3x_1 \leq 18$ ,  $x_1 \leq 8$ ,  $x_2 \leq 6$  and  $x_1, x_2 \geq 0$ .

26) i) Use big -M method to

Minimize  $Z = 2x_1 + 9x_2 + x_3$

Subject to  $x_1 + 4x_2 + 2x_3 \geq 5$ ,  $3x_1 + x_2 + 2x_3 \geq 4$  and  $x_1, x_2, x_3 \geq 0$ .

ii) State complementary slackness theorem of duality.

27) i) Using simplex method, find the inverse of the following matrix

$$A = \begin{pmatrix} 3 & 4 \\ -1 & 2 \end{pmatrix}$$

ii) Show that the feasible solution  $x_1 = 1, x_2 = 0, x_3 = 1$  and  $x_4 = 6$  to the system

$x_1 + x_2 + x_3 = 2$ ,  $x_1 - x_2 + x_3 = 2$ ,  $2x_1 + 3x_2 + 4 = x_4$  is not basic.

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